

Code: CS3T1

**II B.Tech - I Semester – Regular Examinations – December 2015**

**DISCRETE MATHEMATICS  
(COMPUTER SCIENCE AND ENGINEERING)**

Duration: 3 hours

Max. Marks: 70

PART – A

Answer *all* the questions. All questions carry equal marks

11 x 2 = 22 M

1. a) Using the statements : R: John is Healthy  
H: John is clever  
Write the following statements in symbolic form
  - i) If John is healthy then he is not clever
  - ii) John is not healthy but clever.
- b) Construct the truth table for  $\neg(\neg P \wedge \neg Q)$ .
- c) Show that  $(\forall x)(H(x) \rightarrow M(x)) \wedge H(s) \Rightarrow M(s)$ .
- d) Prove that in a lattice  $(L, \leq)$ ,  $a \leq b$  if and only if  $a \wedge b = a$ .
- e) Give an example of a lattice which is distributive but not complemented.
- f) If the universe of discourse is  $\{a, b, c\}$  eliminate the quantifier from the formula  $(\forall x)(P(x))$ .
- g) Define Isomorphism of two graphs.
- h) State Euler's formula for planar Graphs.
- i) Is there a graph with degree sequence (1, 3, 3, 3, 5, 6, 6)?  
Give reasons.

- j) Show that any nontrivial tree contains at least two vertices of degree 1.
- k) Describe the problem of Königsberg Seven bridges and draw its graph.

### PART – B

Answer any **THREE** questions. All questions carry equal marks. 3 x 16 = 48 M

2. a) Show that

$((P \vee Q) \wedge \neg(\neg P \wedge (\neg Q \vee \neg R))) \vee (\neg P \wedge \neg Q) \vee (\neg P \wedge \neg R)$  is a tautology. 8 M

b) Prove that 8 M

$$\neg (p \rightleftarrows q) \iff (p \vee q) \wedge \neg(p \wedge q)$$

3. a) Show that  $(\forall x)(p(x) \vee q(x)) \implies (\forall x)p(x) \vee (\exists x)q(x)$ . 8 M

b) Show that  $r \wedge (p \vee q)$  is a valid conclusion from the premises  $p \vee q$ ,  $q \rightarrow r$ ,  $p \rightarrow m$  and  $\neg m$ . 8 M

4. a) Show that in a lattice  $\langle L, \leq \rangle$  if  $a \leq b \leq c$  then 8 M

i)  $(a \vee b) = (b \wedge c)$ .

ii)  $(a \wedge b) \vee (b \wedge c) = b = (a \vee b) \wedge (a \vee c)$

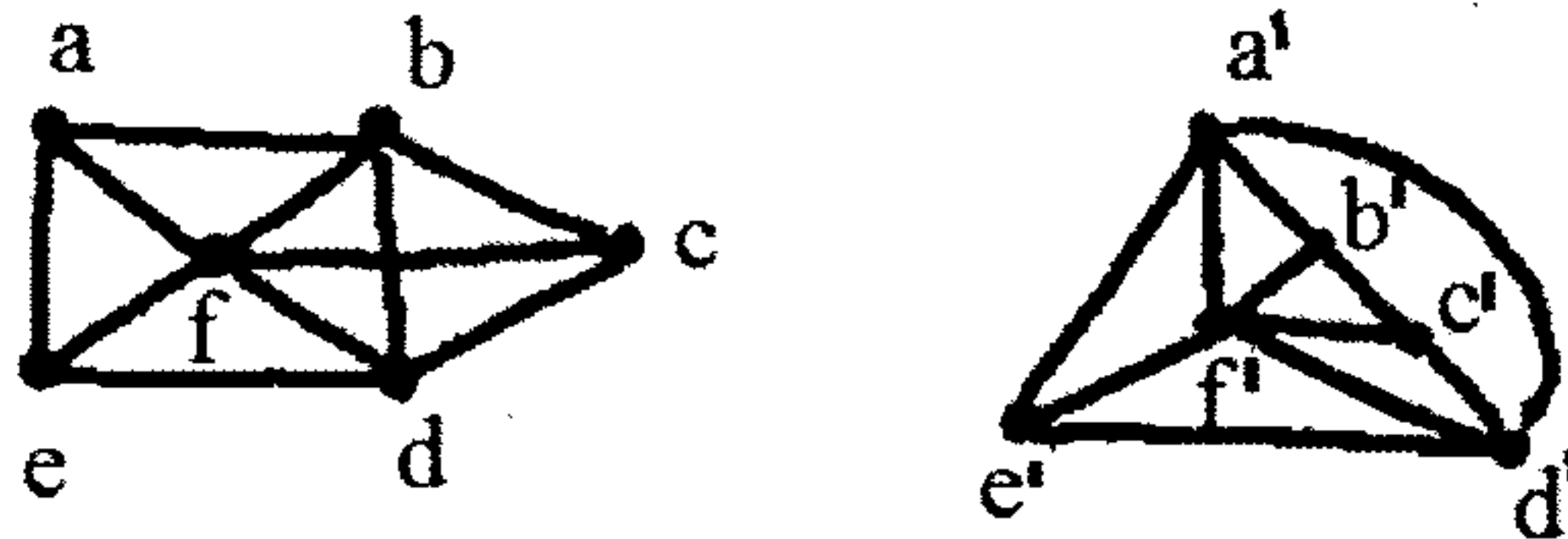
b) i) Prove that every chain is a distributive lattice

ii) Show that every interval of a lattice is sub lattice

8 M

5. a) Are the following pair of graphs isomorphic. Justify your answer.

8 M



b) Prove that every tree with  $n$  vertices has exactly  $(n-1)$  edges.

8 M

6. a) Prove that a complete graph  $K_n$  is planar iff  $n \leq 4$ .

8 M

b) In a connected simple planar graph show that  $|E| \leq 3|V| - 6$

8 M